Solm: Optimize: Distance & Distances (x,1/12), (3,-2,1) Subject to: Sphere -> x21/2+22-4 Equivalent: cpt. d2: (x-3) + (4+2)2+ (2-1)2 } try of legacy multiple hore subj. Sphere > x2142+22-11

But necessary > subunes OOF: (x2-ex+d)+ (2,70H/111)+(5,55+1) cby (X3+45+35-11) Cp.

Obj: (x5145155,)+(d+1/4), (-ex+1/4-5+) CO): 18-6x + 1/4-22 Subj: x2+42+2=4 (7 x2+42+22-4=0

Opt: C(x1412): 18-6x+1/4-22 Subj: g(xy,2)= 0 for g(x,4,2)=x2+42+22-4

W F(x,4,2,2) - (x,4,2) - 2 g(x,4,2) = 18-6x+1/4-22 - 2(x2+y2+22-4)

 $\nabla F = \vec{\delta}$ ∇F

12(x2+ y2, 22) - U2 ie (2x2+ (2y2+ (2y)2+ (12)2= 11/2 multiply (U) by λ^2 . Non abby (1755/13)

(-3)2+ (2)2 + (-1)2 = 4/2 / 1 = 1/2 / 14 = 4/2

Now temember C12: yx = -1(32: yz = -1)

Z Caxs Fa):

if 上京: Hen solving (1)(2)(3) for x, Y, Z

yielding (-3月, 2月, -月)=A

nw F(A): 18-6(-3月)+以(2月)-2(-平)
= 18+28月

if 1.-12: Men solvey (1)(2)(3) for x, y, z yielding (3)(3), -2)(3) = B now f(B)= 18-6(3)(3) +4(-2)(3)-2(1)-2(1)-18-28)(5)

* global optimization comes from local optimization.

:. f(A) > f(B) :. f(A) is futhers+ from (3,-2,1)

.. F(b) is closed to (3,-2,1) via laying right plas.

: Exercise: Find the maximum volume of a box of no lid and scribe a circa R.

| Double Integral |
|--|
| good: integrate firekus d 2 variable |
| (p should an integral mean? |
| in Calc I: can integral. |
| frank "net area of the france |
| m (alc III. If f(x, y) dA Should represent the ret volume Should |
| when the gaph of f ciboux R. |
| - work at simplest possible regions: recetories |
| - work of simplest possible regions records R= [a,b] × [c,d] |
| = {(x, N) X \(\) |
| = S(x'N) X E Tall 21 3 C T Illimination X |
| *m (alc I) R. Ea, b] x [c,d] |
| to compute the definite integral strong and |
| integral standa, ue |
| Chille to where |
| [a,b] and intelligents address |
| orce via "left" enelpoints addressore via "left" enelpoints addressores of height floodpoints) |
| XIN Calc II SI (IX, N) d/ |
| is award. by churking rectagles and |
| is approx. by chenking rectorgles and then probbing some convenience e.g. flower left and probbing |
| for height. It limit the approx. |

Fobri's Theirem: if f(x,y) is c+s on $R = [a,b] \times [c,d]$, then $\frac{y-d}{y-d} \left(\int_{x-a}^{x-b} f(x,y) dx \right) dy = \iint_{R} f(x) dA = \int_{x-a}^{x-b} \left(\int_{y-c}^{x-b} f(x,y) dy \right) dx$ * Start by fixing x as y first. UB: hard in. Ex: Compute SIR x Sec2(y) dA where R= [1,3] , [0, "] Six Seczey) dx dy [2x2 sec(y)], dy 2x2 sec2(y) = 4 sec2(y) 3 43ec2(4) dy = 4 lan(9) (= [4] Other order: 3) [x secrey) dydx -> [x toney) dy (xdx + y) Ex: Comple SS 1+x+y dA on R: [1,2] x [2,3]
SJI: IT THE DE THE SIN THE Jen 13-41-ln 12+4/dy -> 6/n(6) - whis>+4/n(4)-6+5+5-4

= Colon(6)-10ln(5)+4ln(11).